The growth law of primary breast cancer as inferred from mammography screening trials data

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Summary Despite considerable progress in understanding tumour development, the law of growth for human tumours is still a matter of some dispute. In this study, we used large-scale mammography screening trial data to deduce the growth law of primary breast cancer. We compared the empirical tumour population size distributions of primary breast cancer inferred from these data to the distributions that correspond to various possible theoretical growth functions. From this, we showed that the data are inconsistent with the exponential, logistic and Gompertz laws, but support power law growth (exponent = 0.5). This law indicates unbounded growth but with slowing mass-specific growth rate and doubling time. In the clinical size ranges, it implies a greater decline in the mass-specific growth rate than would be predicted by the Gompertz law using the accepted parameters. This suggests that large tumours would be less sensitive to cycle-specific therapies, and be better treated first by non-cell cycle-specific agents. We discussed the use of our study to estimate the sensitivity of mammography for the detection of small tumours. For example, we estimated that mammography is about 30% less sensitive in the detection of tumours in the 1 to 1.5-cm range than it is in detecting larger tumours.

Keywords: breast cancer; mammography screening; cancer growth law; mathematical model

Breast cancer is the most common malignancy in women, afflicting one in every ten women in the Western world. Recently, the role of tumour growth dynamics in determining the clinical course of the disease has been re-emphasized by demonstrating how such knowledge can lead to more efficient treatment protocols (Crowell, 1997). Large-scale breast cancer screening mammography trials show that significantly smaller tumours are detected in screened populations, compared with the control, and it is probable that the disease would be better controlled if smaller tumours could be detected (Tabar et al. 1992; see also Kimmel and Flehinger, 1991 and Xu and Prorok, 1997 for theoretical discussions). Nevertheless, the benefit of screening, especially in younger women (< 50 years), still remains somewhat controversial (Fletcher et al. 1993; Tabar et al. 1995; see also Flehinger et al. 1993 for lung cancer). As interval cancer data indicate that not all prevalent tumours are detected by the screening procedure (Holmberg et al. 1986), any realistic evaluation of mammographic screening efficiency must account for detection sensitivity, particularly for smaller sizes.

In the present work, we employed extensive clinical data from large mammography screening trials that should be representative of the general population. Using mathematical tools, we extracted from these data useful information about breast cancer growth. Our conclusions, corroborated by recent laboratory, clinical and theoretical studies, may be relevant to various aspects of tumour detection and control. In particular, we demonstrate how knowledge of size-dependent tumour growth rates can help evaluate the relative sensitivity of mammography as a function of tumour size. This may be useful for determining the optimal interval between subsequent screenings. In addition, our results may suggest ways to improve chemotherapy treatment protocols.

Previous attempts to estimate human breast cancer growth rates as a function of size were mostly based on those cases in which the primary tumour can be seen in retrospect in previous mammograms. This type of analysis is confined only to very limited and, possibly, not representative groups of patients (Gershon-Cohen et al. 1963; HeUSER et al. 1979; Fournier et al. 1980; Peer et al. 1993; Spratt et al. 1993). Several putative laws for tumour growth have been proposed, based on this type of human study and on experiments in animals. Each of these implies different model-specific dynamics of tumour growth (Mendelsohn 1963; Laird, 1965; Steel and Lamerton, 1966; Norton and Simon, 1976; Norton, 1988).

The most commonly used tumour growth model is exponential growth, in which the cells divide at a constant rate independent of tumour size and age. A more general equation, which represents a very broad family of growth rates (including the exponential), is the power law differential equation:

\[ \frac{dy}{dt} = ky^\beta \]

where \( y \) denotes the tumour mass, \( k \) is a constant of growth and the exponent \( \beta \) is an indicator of the tumour's mode of growth (when \( \beta = 0 \), the growth is linear, when \( \beta = 1 \) the growth is...
exponential, etc.). The solution of the power growth law (equation 1) for \( \beta \neq 1 \) is given by:

\[
y = \frac{1}{(1 - \beta) + c} 
\]

(2)

where \( c \) is a constant. Equation 1 was introduced more than three decades ago by Mendelsohn, and was shown at that time to fit observed growth curves of experimental animal mammary tumours (Mendelsohn, 1963; Dethlefsen et al., 1968).

A different school of thought is represented by the sigmoidal family of functions, such as the logistic and Gompertz growth laws. In these laws it is assumed that tumoral and/or host constraints gradually inhibit tumour growth to an asymptotic value.

Illustrated in Figure 1A are the growth curves that represent the power law model, with \( \beta = 1 \) (exponential growth) and \( \beta = 0.5 \) (parabolic growth), as well as Gompertz growth. The exponential and Gompertz curves have been plotted using accepted parameters drawn from the literature (Fourier et al., 1980; Norton, 1988). Figure 1B shows that these models predict remarkably different time-dependent changes in the mass-specific tumour growth rate. Determining which function is most suitable for describing primary breast cancer growth is therefore warranted.

**METHODS**

**Calculating the probability that a tumour is detected before screening**

Consider a tumour of size \( z \) that would be present in a natural population with no removals. This tumour, in the actual screen population, might be detected and removed before screening: we wish to calculate the probability \( p \) of this detection. Let \( \mu(v) \) be the probability density (with respect to tumour size) that a tumour is detected at size \( v \). Then the probability of detection before the tumour reaches size \( s \) is:

\[
p = \frac{1}{s} \int_{0}^{s} \mu(v) dv 
\]

We can estimate the value of this integral using the data for the control population. These data consist of the number \( n_k \) of tumours detected between sizes \( v_{k-1} \) and \( v_k \) for each of the \( m \) size categories, \( k = 1, 2, …, m \). The probability density \( \mu \) in the \( k \)th size class is thus approximately:

\[
\mu(v) = \frac{n_k}{m(v_k - v_{k-1})} 
\]

where \( n = \sum n_k \) is the total number of tumours detected in the control population. The tumour of size \( s \) will be on average approximately in the middle of its size category \( k \). Thus, the above integral can be approximated as:

\[
p = \left[ \frac{1}{m} \sum_{k=1}^{k-1} \frac{n_k}{m(v_k - v_{k-1})} (v_k - v_{k-1}) \right] + \frac{n_k}{m(v_k - v_{k-1})} \cdot \frac{v_k - v_{k-1}}{2} = \left[ \frac{1}{m} \sum_{k=1}^{k-1} \frac{n_k}{n} \right] + \frac{n_k}{2n}
\]

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Theoretical distributions of tumour sizes in populations

The growth rate of solid tumours depends on a multiplicity of factors, such as vascularity and nutrient supply, interactions with surrounding tissues, growth factors, regulation of apoptosis, and so on. These factors themselves vary with tumour size. Thus, the rate of growth of the tumour can be considered as a function of size. To express this in mathematical terms, let \( y(t) \) denote the tumour mass at time \( t \). Then the tumour will grow according to some differential equation of the form:

\[
\frac{dy}{dt} = f(y)
\]

where \( f \) is some differentiable function of the tumour mass \( y \).

We wish to derive the probability density \( \varphi (y) \) that a tumour, randomly chosen from a certain size range and growing according to the differential equation (3), is of size \( y \) assuming no removals due to treatment or death. It will also be assumed that the distribution of tumours, \( \varphi (y) \), is stationary, i.e. the probability density of tumours is independent of time. This is reasonable for populations that are fairly stable demographically, and for which there has been no 'point event' (such as an acute exposure to radiation or other carcinogens) that would cause an unusually large number of tumours to be formed at about the same time.

Consider the population of tumours whose masses lie in the interval \( y \) and \( y + \Delta y \). Tumours are entering this population at the rate:

\[
\frac{dy}{dt} = \varphi (y) f(y)
\]

they are leaving the population at the rate:

\[
\varphi (y + \Delta y) f(y + \Delta y) = \varphi (y + \Delta y) (f(y) + f'(y) \Delta y) + o(\Delta y)
\]

Equating these two quantities and rearranging gives:

\[
\frac{\varphi (y + \Delta y) - \varphi (y)}{\Delta y} = - \varphi (y) + \frac{f'(y)}{f(y)} + o(\Delta y)
\]

so taking the limit as \( \Delta y \to 0 \) gives the differential equation:

\[
\varphi' (y) = - \frac{\varphi (y)}{y} f'(y) + \frac{f'(y)}{f(y)}
\]

Equation 5 has the general solution:

\[
\varphi (y) = \frac{C}{f(y)}
\]

where \( C \) is a constant chosen to normalize the probability density to one. In the case of power law growth (equation 1), \( f(y) = ky^\beta \), and hence

\[
\varphi' (y) = -\beta \varphi (y) + \varphi (y)
\]

Using equation 6, equation 7 becomes

\[
\varphi (y) = \frac{C}{y^\alpha}
\]

Note that as this result does not depend on the tumour growth rate parameter \( k \), it is valid even when (as is actually the case) \( k \) varies in the population, provided the distribution of \( k \) values is also stationary.

Gompertz growth satisfies the differential equation:

\[
\frac{dy}{dt} = k_s e^{-\alpha y}
\]

where \( k_s \) and \( \alpha \) are constants. This equation can be transformed into the autonomous form of equation 3 with \( f \) given by:

\[
f_r (y) = -\gamma \ln \left( \frac{y}{K} \right)
\]

where \( K \) is the limiting size of the tumour and \( \gamma \) is a constant (Edelstein-Keshet, 1988). Inserting this into equation 6 gives:

\[
\varphi (y) = \frac{C}{y \ln \left( \frac{y}{K} \right)}
\]

The logistic differential equation is:

\[
\frac{dy}{dt} = r y \left( 1 - \frac{y}{K} \right)
\]

where \( r \) and \( K \) are constants, representing the intrinsic growth rate and the limiting size of the tumour respectively. From equation 6 we have:

\[
\varphi (y) = \frac{C}{y (K - y)}
\]

The graphs of the theoretical distributions derived in equations 8, 11 and 13 with best fit of the two-county Swedish data are shown in Figure 2.

RESULTS

We focused our analysis on the size distribution of tumours found in the first screen of the two-county Swedish mammography trial, which is one of the largest and most detailed studies of its kind (Tabar et al., 1992). Other published mammography screening trials (Thomas et al., 1984; Fagerberg et al., 1985; Barbken et al., 1992; Peer et al., 1994; de Koning et al., 1995) are less detailed, but can provide valuable information about the tumour size distribution (Table 1).

Our first aim was to reconstruct from the two-county Swedish mammography data the natural tumour size distribution in the population, i.e. what the size distribution would have been had there been no removals before the first screen. To this end, we employed the distribution of tumour sizes at detection in the two-county Swedish study’s large corresponding control group. We reconstructed the natural tumour size distribution by estimating the probability, \( p \), that a tumour of a given size category would have been detected without screening (see Methods), and then divided the number of tumours detected by mammography in each category by \( 1 - p \). We excluded from the analysis the smallest (< 1 cm) size category because of reduced mammography sensitivity in small tumours (Feig et al., 1977; Yaffe et al., 1993). As the probability of self-detection in the largest size category (> 5 cm) is close to 1, dividing by \( 1 - p \) would produce a number extremely sensitive to the exact value of \( p \), and thus be unreliable; therefore, this size category was excluded as well (Table 1). We assumed that in the 1- to 5-cm range there is little variation in detection sensitivity (with the possible exception of the 1- to 1.5-cm category). Hence, we took the probability of detection in these size categories as constant.

Figure 2  The best fit of the theoretical density distributions of tumour size (equations 8, 11 and 13) to the reconstructed natural distribution estimated from the two-county Swedish data (Tabar et al., 1992) A. Results are presented on a log-log plot. A highly significant linear fit of the data was obtained with a slope \( \beta = -0.42 \) \((r^2 = 0.97)\). The Gompertz law was fitted using a limiting size of 3100 ml (Norton, 1988). The logistic growth was fitted using a limiting size of 1000 ml estimated by Spratt et al (1993).

Figure 3  Estimation of mammography sensitivity in small tumours (0.5–1.5 cm). The theoretical density distribution of tumour size (assuming power law growth, equation 8) was fitted to the two-county Swedish data (in the 1.5–5.0 cm range) A and subsequently was extrapolated to the smallest tumour range. The ratio between the theoretical and the empirical points can be readily converted to the relative probability of detection. The mammography in the 1–1.5 cm range detects at most 70% of the prevalent tumours. In the 0.5–1 cm range no more than 40% of the tumours are detected. Results are presented on a log-log scale.

Table 1  Size distribution of screened, control and reconstructed natural tumour populations, obtained from published breast cancer screening trials. Only the first screen data for tumours are used. The probability density \( P \) for a tumour between 1 and 5 cm in a natural population to be found in a particular size category is estimated. The results of linear regression of the log-log of the natural tumour size distribution vs the log-log of the relevant tumour volumes (linear slope \(-\beta\)) and the corresponding \( r^2 \) are presented. For those data sets where the number of data points was not sufficient to perform a regression analysis, only the linear slopes were calculated.

<table>
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<th>Source</th>
<th>Tumour size (cm)</th>
<th>No. of screen</th>
<th>No. of control</th>
<th>Probability density ( P )</th>
<th>(-\beta)</th>
<th>( r^2 )</th>
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*aTumour diameters as reported in the source articles. *Number of detected cancers in the group. \( P \) in data sets with no control population, the Swedish control incidence rates were used. **Probability density is the reconstructed natural probability density for the tumour population between 1 and 5 cm (0.6 and 5 cm in Guildford).*
We compared this empirical distribution with the theoretical distributions of primary tumour volumes corresponding to power, Gompertz and logistic growth laws (see Methods). Figure 2 displays the best-fit plots of these theoretical distributions to the reconstructed natural distribution obtained from data of the two-county Swedish trial (Tabar et al. 1992). The points calculated from the trial data lie nearly on a straight line with slope $\beta = -0.42$ ($r^2 = 0.97$), indicating a power law growth function with $\beta = 0.42$. Note that these data are inconsistent with exponential growth (power law with $\beta = 1$), nor are they consistent with Gompertz or logistic growth laws with the accepted limiting sizes (Norton, 1988; Spratt et al. 1993). Most of the non-linearity in the two-county Swedish data is due to the density of the lowest size category (1-1.5 cm), where the sensitivity of the mammography may be less than for larger tumours. Excluding this point gives a slightly higher exponent ($\beta = 0.53$; $r^2 = 0.99$). Thus, the evidence indicates that primary breast cancer growth is parabolic (power law growth, $\beta = 0.5$).

Verification of the result using independent screening trials

We verified our result by using data from other published mammography screening trials; only studies that contain sufficient information for analysis were included. Our analysis of these data, including an earlier report of the same Swedish study discussed above (Fagerberg et al. 1985), give consistent results: the data in all cases are compatible with power law growth, with $\beta$ between 0.32 and 0.55 (Table 1). The slopes of the UK (Thomas et al. 1984) and British Columbia (Burhenne et al. 1992) trials ($\beta = 0.32$ and $\beta = 0.38$) are even more contradictory to the Gompertz law. However, as these trials did not have their own control groups, they are less reliable. If Swedish women were more careful about regular self-examination, there would be more large tumours removed before screening compared with the British or the British Columbian studies. In such a case the probability of detection before screening, $p$, in the larger size classes would be overestimated by the use of the two-county Swedish control, so the slope would be underestimated. Note that in all the controlled studies the slope ranged between 0.41 and 0.54. It appears, then, that a control group in each screening trial is important for the use of this technique.

DISCUSSION

Our results suggest that tumour size increases approximately as a quadratic function of time (i.e., parabolic growth). This is slower than exponential, but without the limiting asymptotic size suggested by sigmoidal growth models. Parabolic growth indicates a mass-specific growth rate that declines with the square root of tumour mass, as opposed to the constant mass-specific growth rate of exponential growth. Whereas the Gompertz and the logistic laws also predict a slowing mass-specific growth rate, these declines, using the parameters estimated in Norton (1988) and Spratt (1993), are less significant in the clinical size ranges than those predicted by parabolic growth (Figure 1B). This may imply that the response of breast cancer to chemotherapy may be different than would be suggested by the Norton–Simon model that assumes Gompertz growth (Norton and Simon, 1986).

There is substantial evidence at the cellular level of a decline in the mass-specific growth rate as tumours increase in size. Studies of the cytokinetics of both human breast cancer and experimental tumours show that the thymidine labeling index (TLI) declines in larger tumours, indicating that the fraction of cells that are actively growing is decreasing (Schiöffer et al. 1979; Meyer and Coplin, 1988). Recent reports indicate that the vascular density of tumours may decline with growth (Holmgren et al. 1995). In such a case a significant fraction of tumour cells that lie too far from a capillary will be driven to a non-proliferating state or possibly even to death.

It should be emphasized that our method does not require knowledge of the absolute sensitivity of detection. Rather, in this work we made a simple and not unreasonable assumption that the sensitivity in the 1–5 cm size range is approximately constant. If independent measures of mammography sensitivity could be obtained (e.g. by comparing with magnetic resonance imaging (MRI)), it would be possible to use our method for estimating the tumour growth law for smaller size categories.

Alternatively, assuming that the parabolic growth law holds for the smaller size categories, the results of this study can be used for estimating the relative sensitivity of mammography in smaller tumours. This can be done by observing the deviation from linearity in these size categories in the log–log tumour size distribution plot. For example, it appears, by analysing data from the two-county Swedish trials, that mammography in the 1–1.5 cm range is about a third less sensitive than for larger tumours (Figure 3). By extrapolating the regression line to 0.5- to 1-cm range, we estimated that the relative sensitivity of mammography in this size range is about 40% (assuming $\beta = 0.42$) or about 30% (assuming $\beta = 0.53$) compared with larger tumours. This type of sensitivity analysis, combined with the power law for breast cancer growth, may help determine the optimal time period between screening mammography.

This study also may have implications for breast cancer cell kinetic parameter estimation. For instance, the tumour’s potential doubling time and cell loss factor, which may be useful for dose calculation in radiotherapy, are calculated under the assumption of a constant cell cycle time and an exponential tumour growth, respectively (Steel, 1967, 1989; Bertuzzi et al. 1995). If, as our study suggests, tumours follow parabolic growth, it would be necessary instead to estimate the patient-specific growth constant, $k$ (equation 1), which is probably highly variable (Fournier et al. 1980).

Alternating chemotherapy regimens, proposed by Goldie and Coldman for minimizing the risk of drug resistance (Goldie and Coldman, 1979), have been the rationale of numerous anti-cancer protocols for the last 20 years. Our findings may imply an alternative strategy. If, as our results suggest, there is a significant decline in the percentage of actively dividing cells in large tumours (Figure 1B), these tumours would be less sensitive to cycle-specific therapies. Therefore, they may be better treated first with rather broader activity antineoplastic drugs, such as anthracyclines or alkylating agents. This may be an explanation for the observation that alternating the non-cell cycle-specific drug, doxorubicin, with CMF (cyclophosphamide, methotrexate, 5-fluorouracil, the last two drugs being cell cycle specific) is significantly inferior to a sequential chemotherapy protocol with doxorubicin as the first drug for high-risk (i.e. large tumour burden) breast cancer (Bonadonna et al. 1995).

Our results refer to the growth of untreated tumours only and their relevance for the growth patterns of tumours under treatment remains to be investigated. Nevertheless, it is interesting to note that the relative benefit of accelerated irradiation strategy (Corvo et al. 1995) may be explained in part by our results. If irradiated tumours are subject to a similar power law growth, according to which as
tumours shrink under treatment their growth fraction increases, then the latter period of therapy should be more aggressive. The optimal growth patterns of interacting cell assemblies have recently been shown to follow parabolic or other power laws (Drasdo et al. 1995). These theoretical results corroborate our analysis of clinical data, and imply that power growth law may have greater generality than just to mammmary tumours. Our very preliminary analyses of thyroid cancer and renal cell carcinoma screening data suggest that the growth rate of these tumours may also follow a power law. More empirical evidence is needed to assess the universality of power law growth and its usefulness in the control of cancer.

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REFERENCES


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